

# Analysis of A Xi-minus Hyperon Inflight Decay Event

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## Abstract

In this research, a Xi-minus hyperon inflight decay event which was found in nuclear emulsion of KEK E373 experiment had been analyzed. The kinetic energy and momentum of Xi-minus hyperon that was the entering point into nuclear emulsion were estimated by using the range and angle information of Xi-minus and its decay daughters,  $\pi^-$  and  $\Lambda$ . The obtained values of kinetic energy and momentum were 56.69 MeV and 391.18 MeV/c, respectively.

Key Words: Xi-minus hyperon, inflight decay, nuclear emulsion

## Introduction

The Xi-minus ( $\Xi^-$ ) hyperons were produced via quasi free 'p' ( $K^-, K^+$ )  $\Xi^-$  reaction in a diamond target with 1.66 GeV/c  $K^-$  meson beam in KEK E-373 Experiment. Emitted  $\Xi^-$  hyperons were entered into nuclear emulsion stack which was situated at the downstream of diamond target. One stack of emulsion was composed of one thin plate (plate #1) with thickness  $\sim 400 \mu\text{m}$  and 10 or 11 thick plates with thickness  $\sim 1050 \mu\text{m}$  (plate #2 to #11 or #12). The area of emulsion plates was  $24.5 \times 25.0 \text{ cm}^2$ . Total 100 stacks (module) were used in E373 experiment. Some  $\Xi^-$  hyperons were brought to rest in nuclear emulsion and captured by emulsion nuclei and could found compound nucleus with strangeness quantum number  $S = -2$ . At the decay of the compound nucleus, a double  $\Lambda$  hypernucleus, twin single  $\Lambda$  hypernucleus, single  $\Lambda$  hypernucleus and H di baryon (if exist) were emitted. On the other hand, some  $\Xi^-$  hyperon inflight decayed into  $\pi^-$  meson and  $\Lambda$  hyperon which can be seen thin track ( $\pi^-$ ) at the end of straight thick track ( $\Xi^-$ ) in nuclear emulsion. Track of  $\Lambda$  hyperon cannot be seen in nuclear emulsion because it has no charge. A schematic view of  $\Xi^-$  hyperon inflight decay event and around the target region of E 373 experiment is shown in Figure (1). We chose an event in which  $\pi^-$  meson track was stopped at Scintillating Micro Fiber Block (SciFi-Block) detector. This event was found in plate #7 of Module #65. We measured the range of  $\pi^-$  meson track not only in nuclear emulsion (pl #7 to #12) but also in downstream of SciFi-Block. Moreover, the range of  $\Xi^-$  hyperon track from plate #7 to plate #1 was measured. We obtained the angle between the  $\Xi^-$  hyperon track and  $\pi^-$  meson track. The kinetic energy and momentum of  $\Xi^-$  hyperon's decay point was obtained from the range, kinetic energies of its decay daughter and conservation laws of energy and momentum. Finally, kinetic energy and momentum of  $\Xi^-$  hyperon at its entering point into nuclear emulsion (pl#1) was estimated from measured range data (from pl #7 to pl#1) and its decay point data.

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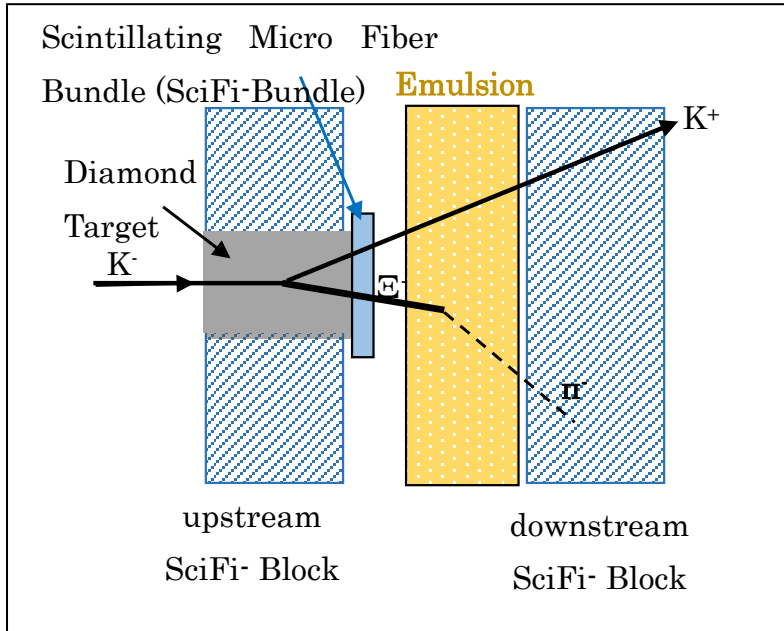


Figure (1) A schematic view of  $\Xi^-$  hyperon inflight decay event and around the target region of E 373 experiment

**Event Description, Range Measurements and Event Reconstruction**

**Event Description of A Xi-minus Hyperon Inflight Decay in Nuclear Emulsion**

The photograph and schematic drawing of  $\Xi^-$  hyperon inflight decay event are shown in Figure (2). The  $\Xi^-$  hyperon entered and then inflight decayed at point A, from which  $\pi^-$  meson and invisible lambda ( $\Lambda$ ) hyperon were emitted.  $\pi^-$  meson track was left the emulsion stack and stopped in SciFi-block detector which was placed downstream of the emulsion chamber. The SciFi image for stopped  $\pi^-$  meson track in his event is shown in Figure (3). Four black spots in D- Block image express the stopped  $\pi^-$ .

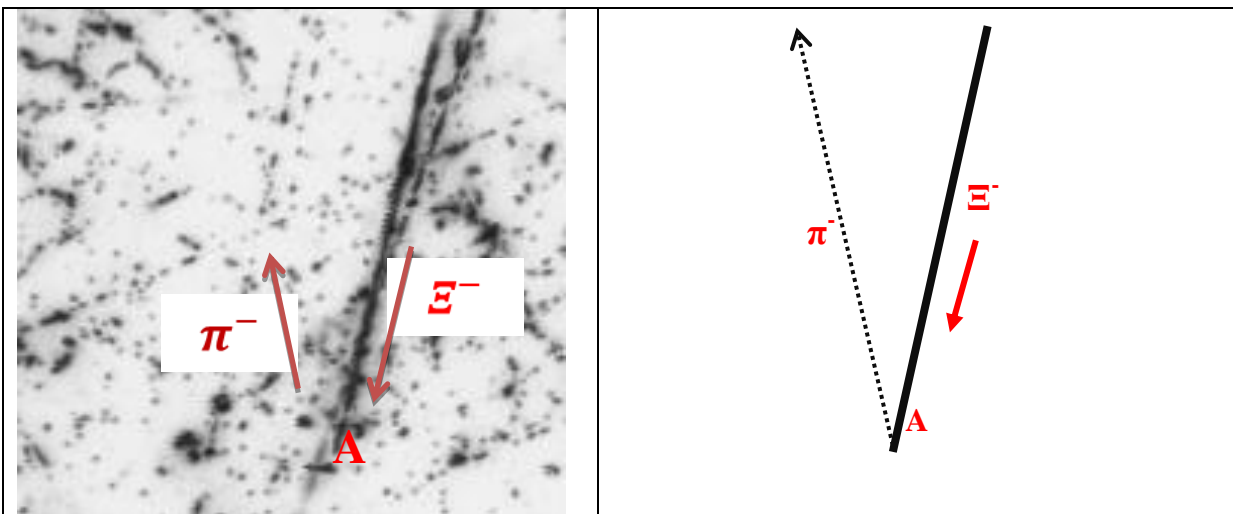


Figure (2) A photograph and schematic drawing of a xi-minus hyperon inflight decay event

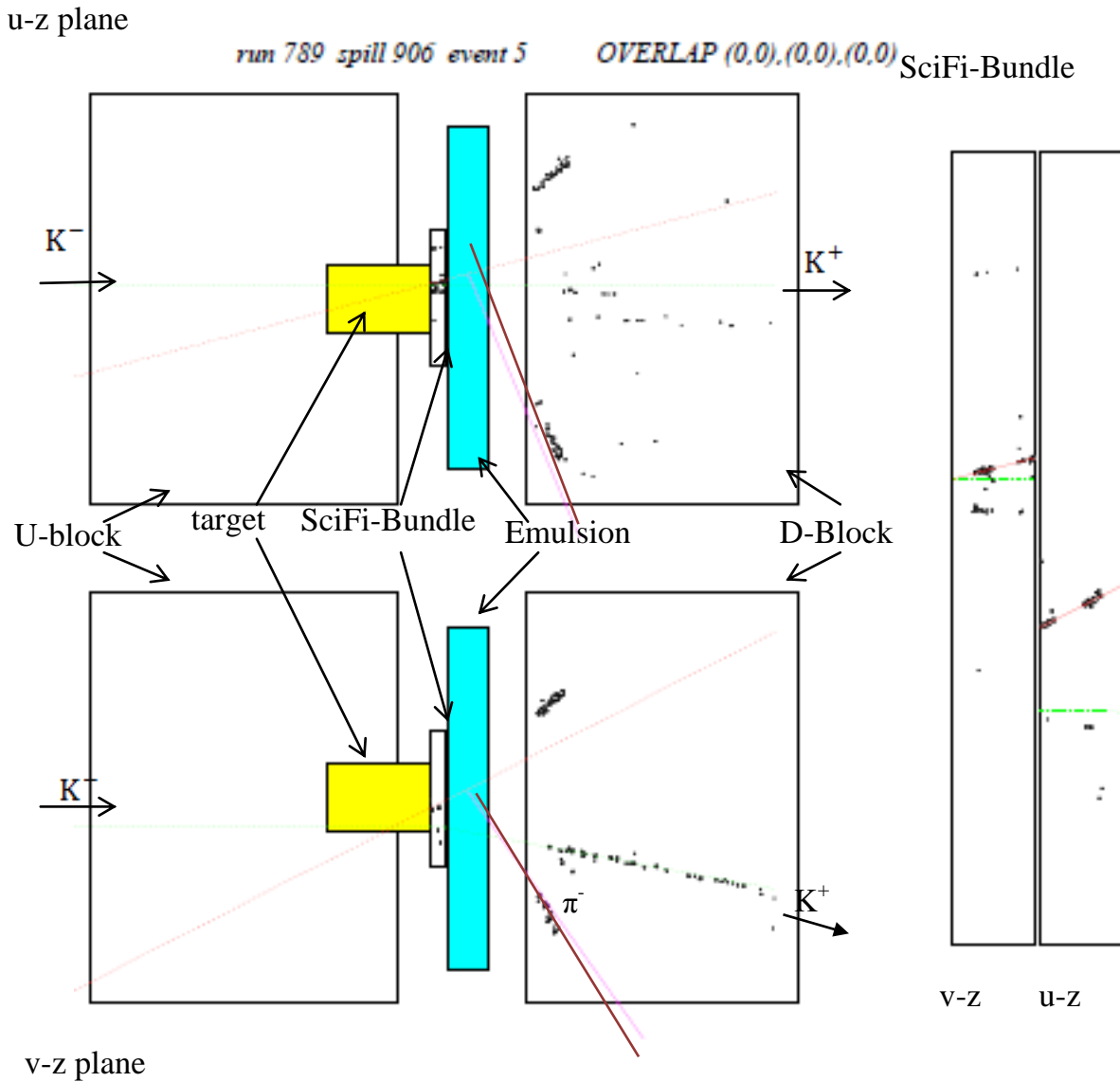


Figure (3) The SciFi image for stopped  $\pi^-$  meson track

**Range and Angle Measurement of Xi-minus Hyperon and  $\pi^-$  Meson**

We measured the range of  $\Xi^-$  hyperon (pl #7 to pl #1) and  $\pi^-$  meson (pl #7 to pl #12) tracks in emulsion by using the microscope system. The range of the track, R can be obtained from measured x, y, z coordinates by using the following relation.

$$R = \sqrt{\Delta x^2 + \Delta y^2 + \Delta z^2} \cdot S \tag{1}$$

Where,  $\Delta x$ ,  $\Delta y$  and  $\Delta z$  were the length of the track in the x, y and z direction respectively. The S was the shrinkage factor. We also obtained the angle between  $\Xi^-$  hyperon and  $\pi^-$  meson tracks by using equation (2).

$$\vec{\Xi}^- \cdot \vec{\pi}^- = |\vec{\Xi}^-| \cdot |\vec{\pi}^-| \cos \theta \tag{2}$$

Since the  $\pi^-$  meson track was left from the emulsion plate and stopped in downstream of SciFi-Block, we needed to obtain range in SciFi and transform into corresponding range in

nuclear emulsion. The range of the  $\pi^-$  meson track was obtained from the size of D-Block in u, v, z directions (120 mm× 120 mm× 80 mm). The corresponding kinetic energy was obtained by using the range energy relation equation in SciFi-Block detector.

$$R = a \times T^b \tag{3}$$

Where  $a$  and  $b$  were the fitting parameter. The values of “ $a$ ” and “ $b$ ” are, 0.107 and 1.62, respectively. We considered again that the range in nuclear emulsion for that energy value of  $\pi^-$ . Because SciFi-Block and nuclear emulsion were different media.

**Event Reconstruction**

The  $\Xi^-$  hyperon was identified from event reconstruction of its decay at point A. We assumed that  $\Xi^-$  hyperon inflight decayed into a  $\pi^-$  meson and another neutral particle, a  $\Lambda$  hyperon. We considered the kinematic of decay event where the direction of  $\Xi^-$  hyperon as x-axis is shown in the following Figure (4).

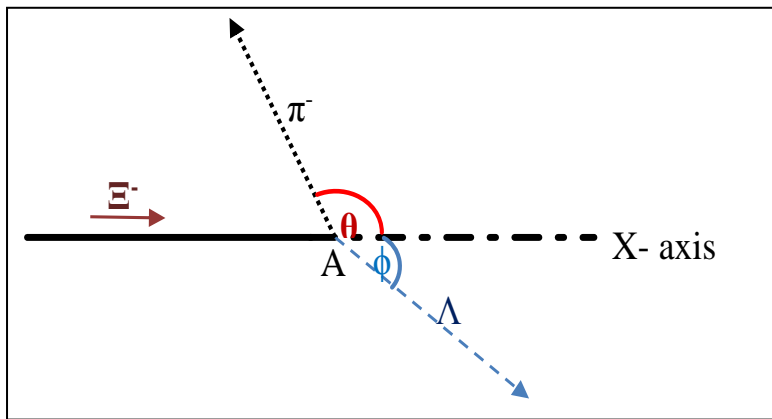


Figure (4) The kinematic of decay event

Firstly, we considered the decay point of  $\Xi^-$  hyperon, point A in Figure (4). Invariant mass of  $\Xi^-$  hyperon was obtained from the information of its decay daughters,  $\pi^-$  meson and  $\Lambda$  hyperon, by using the following Equation (3).

$$M_{\Xi^-}^2 = \left( \sqrt{M_{\pi^-}^2 + P_{\pi^-}^2} + \sqrt{M_{\Lambda}^2 + P_{\Lambda}^2} \right)^2 - (P_{\pi^-} \cos\theta + P_{\Lambda} \cos\phi)^2 \tag{4}$$

The values of  $\phi$  were obtained from momentum conservation relation,  $P_{\pi^-} \sin\theta = P_{\Lambda} \sin\phi$  by inserting the various value of  $P_{\Lambda}$ . And then, we deduced the momentum of  $\Xi^-$  hyperon at point A from the following momentum conservation relation,

$$P_{\Xi^-} = P_{\pi^-} \cos\theta + P_{\Lambda} \cos\phi \tag{5}$$

The value of momentum and kinetic energy for  $\Xi^-$  hyperon at point A were obtained. Then, we calculated the corresponding range in nuclear emulsion by using energy-range program. The total range of  $\Xi^-$  hyperon was obtained from estimated range at point A plus measured range from pl #7 to pl #1. Finally, we calculated the kinetic energy and momentum of  $\Xi^-$  hyperon at plate#1 from its total range by using range- energy program.

## Results and Discussions

### Result of Range Measurement of $\Xi^-$ hyperon and $\pi^-$ meson in Nuclear Emulsion

We measured the range of  $\Xi^-$  hyperon and  $\pi^-$  meson in decay event of #9501-3 which was found in nuclear emulsion plate of #7, Mod # 65 of KEK E373 experiment by using the microscope system. The range of  $\Xi^-$  hyperon from Pl#7 to Pl#1 was measured. Similarly, the range of  $\pi^-$  meson from Pl#7 to Pl # 12 was measured. The range of each track was obtained from measured coordinates by using the Equation (1). The range of  $\Xi^-$  hyperon in nuclear emulsion was 6700  $\mu\text{m}$  and that of  $\pi^-$  meson was 18700  $\mu\text{m}$ .

### Result for Estimation of Range and Kinetic Energy of $\pi^-$ meson in Down Stream of SciFi Block

$\pi^-$  meson track was left the emulsion stack and stopped in downstream block (D-Block) of Scintillation Microfiber block (SciFi-block) detector. The ranges of tracks in SciFi-Blocks can be obtained by using the size of D-Block in u, v, z directions, 120 mm  $\times$  120 mm  $\times$  80 mm. The range of the  $\pi^-$  meson track which was emitted from decay event in D-Block was 21.8 mm (21800  $\mu\text{m}$ ). The corresponding kinetic energy was obtained by using the range energy relation equation, Equation (3), in SciFi-Block detector. The kinetic energy of  $\pi^-$  meson track would be 26.7 MeV.

### Result for Estimation of Total Range and Kinetic Energy of $\pi^-$ meson

Since the kinetic energy of  $\pi^-$  meson track in Sci-Fi block was 26.7 MeV. We considered that the range of  $\pi^-$  meson track in nuclear emulsion if it has 26.7 MeV, kinetic energy. The corresponding range in nuclear emulsion was obtained by using the energy-range program for nuclear emulsion which was based on Barks's literature. The range obtained by using range energy relation in nuclear emulsion was 13284.30  $\mu\text{m}$ . The total range of  $\pi^-$  meson track which included range in emulsion as well as in Sci-Fi block was 31984  $\mu\text{m}$ . Its kinetic energy was 45.25 MeV. The symmetrized range and kinetic energy for  $\pi^-$  meson were expressed in Table 1.

Table 1. The symmetrized range and kinetic energy for  $\pi^-$  meson

Range in Emulsion ( $\mu\text{m}$ ) (pl# 7 ~ 12)	Range in Sci-Fi Block ( $\mu\text{m}$ )	Kinetic Energy in Sci-Fi Block (MeV)	Corresponding Range in Emulsion ( $\mu\text{m}$ )	Total Range of $\pi^-$ meson ( $\mu\text{m}$ )	Total Kinetic Energy of $\pi^-$ meson (MeV)
18700	21800	26.7	13284.3	31984.3	45.3

### Result for Estimation of Momentum of $\Lambda$ hyperon

Decay event was reconstructed at  $\Xi^-$  hyperon decay point by using the conservation laws of energy and momentum. We imagined that  $\Xi^-$  hyperon was decay into  $\pi^-$  meson and  $\Lambda$  hyperon at point A. The invariant mass of  $\Xi^-$  hyperon was obtained by using Equation (4) with the information of decay daughters. The value of  $\phi$  were deduced from momentum

conservation relation,  $P_{\pi} \sin\theta = P_{\Lambda} \sin\phi$  by inserting the various value of momentum of lambda hyperon  $P_{\Lambda}$  which was from minimum value 113.6 MeV/c to 350.6 MeV/c. The various value of mass of  $\Xi^-$  hyperon obtained from corresponding momentum of  $\Lambda$  hyperon, as shown in Figure (5). The invariant mass of  $\Xi^-$  hyperon,  $M_{\Xi^-} = 1321.31\text{MeV}/c^2$ , was obtained at momentum of  $\Lambda$  hyperon,  $P_{\Lambda} = 330.10$  MeV/c. The kinetic energy and momentum of  $\pi^-$  meson,  $\Lambda$  hyperon and  $\Xi^-$  hyperon at point A are summarized in Table 2.

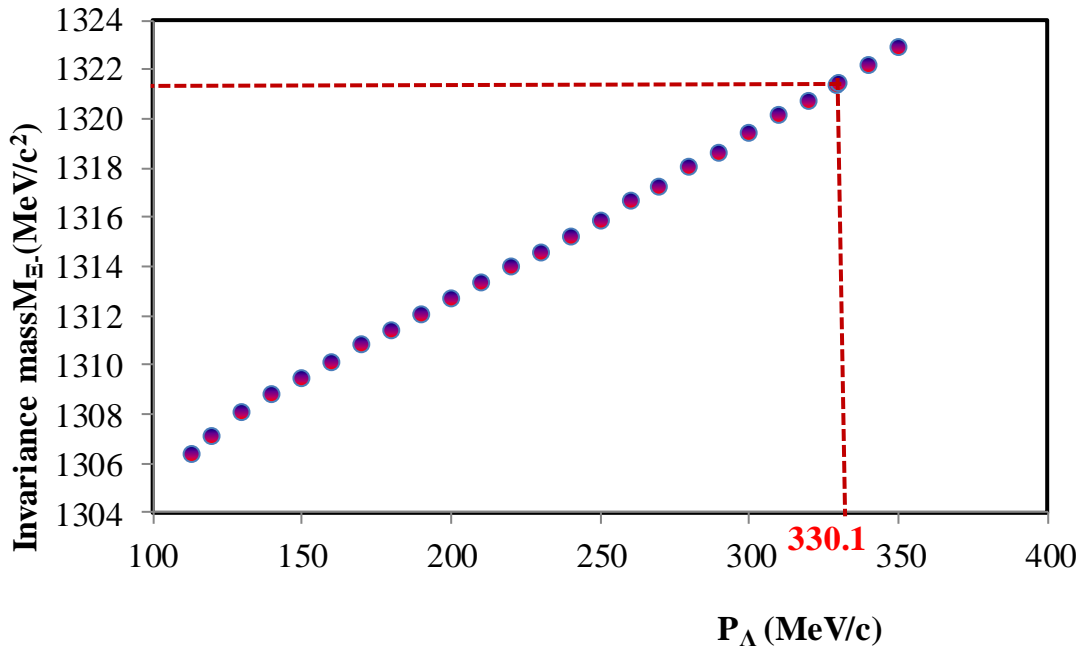


Figure (5) Invariance mass of  $\Xi^-$  hyperon and momentum of  $\Lambda$  hyperon

Table 2. The kinetic energy and momentum of  $\pi^-$  meson,  $\Lambda$  hyperon and  $\Xi^-$  hyperon at point A.

$\pi^-$		$\Lambda$		$\Xi^-$	
Kinetic energy (MeV)	Momentum (MeV)	Kinetic energy (MeV)	Momentum (MeV/c)	Kinetic energy (MeV)	Momentum (MeV)
45.3	121.155	48.8	330.10	27.3	268.5

### Result for Determination of Kinetic Energy and Momentum of $\Xi^-$ hyperon at Plate#1

The momentum and kinetic energy of  $\Xi^-$  hyperon at point A were obtained by using the momentum conservation and energy-momentum relations. Its values have to be 68.5 MeV/c and 27.3 MeV, respectively. The range of  $\Xi^-$  hyperon obtained from kinetic energy at point A was 2578.73  $\mu\text{m}$ . The range of  $\Xi^-$  hyperon from point A at plate #7 to plate #1 was 6700  $\mu\text{m}$ . The total range of  $\Xi^-$  hyperon was 9278.73 $\mu\text{m}$ . The kinetic energy and momentum of  $\Xi^-$  hyperon at plate#1 were 56.7 MeV and 391.2 MeV/c respectively. The symmetrized range, kinetic energy and momentum of  $\Xi^-$  hyperon were expressed in Table 3.

Table 3. Range, kinetic energy and momentum of  $\Xi^-$  hyperon at point A and at Pl#1

Kinetic Energy of $\Xi^-$ at point A (MeV)	Corresponding Range ( $\mu\text{m}$ )	Range of $\Xi^-$ Pl#1 to Pl#7 ( $\mu\text{m}$ )	Total Range of $\Xi^-$ hyperon ( $\mu\text{m}$ )	Kinetic Energy of $\Xi^-$ hyperon at Pl#1 (MeV)	Momentum of $\Xi^-$ hyperon at Pl#1 (MeV/c)
27.3	2578.73	6700	9278.73	56.7	391.2

## Discussions

The event reconstruction in nuclear emulsion is based on the conservation laws of energy and momentum. A  $\Xi^-$  hyperon decayed into a charged particle and some neutral one at point A. The emitted particle from event left the emulsion stack and stopped in downstream of SciFi-Block (D-block). That particle was identified as a  $\pi^-$  meson because of the mean brightness value of the track. We measured the range of tracks in  $\Xi^-$  hyperon decay event. We obtained the angle between the  $\Xi^-$  hyperon and  $\pi^-$  meson. The kinetic energy and momentum of  $\pi^-$  meson was obtained from the total range which included range in emulsion plus corresponding range in emulsion changed from range in Sci-Fi block by using the range energy relation. And then, we also calculated the invariant mass of  $\Xi^-$  hyperon by using the various value of  $P_A$  and  $\phi$  based on momentum conservation relation. The value of  $\phi$  was obtained by using this equation  $P_\pi \sin \theta = P_A \sin \phi$  and inserting the various value of  $P_A$ . Then, we estimated momentum and kinetic energy of  $\Xi^-$  hyperon at point A. The momentum and the kinetic energy were 268.5 MeV/c and 27.3 MeV, respectively. The corresponding range in nuclear emulsion, 2578.73  $\mu\text{m}$ , was obtained by using the energy-range program. The measured range of  $\Xi^-$  hyperon from plate#1 to #7 was 6700  $\mu\text{m}$  by using microscope system. Then, total range of  $\Xi^-$  hyperon was 9278.73  $\mu\text{m}$ . Finally, the kinetic energy and momentum of  $\Xi^-$  hyperon at plate#1 were 56.7 MeV and momentum was 391.2 MeV/c respectively.

## Conclusion

We have analyzed one of the decay events in nuclear emulsion of E373 experiment. The decay event is the cascade decay of,  $\Xi^- \rightarrow \pi^- + \Lambda$ ;  $\Lambda \rightarrow p + \pi^-$ . However,  $\Xi^- \rightarrow \pi^- + \Lambda$  decay mode can be detected in nuclear emulsion of E373 experiment. We measured the range of  $\pi^-$  meson not only in emulsion but also in SciFi-Block detector. We obtained the kinetic energy and momentum of  $\pi^-$  meson from its range. Moreover, the momentum of  $\Lambda$  hyperon was estimated. In our analysis, the momentum of  $\Xi^-$  hyperon at pl#1 was estimated by using the information of its decay daughter,  $\pi^-$  and  $\Lambda$ , based on the conservation laws of energy and momentum.

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